



REGISTRATION NUMBER

| | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|
| | | | | | | | | | |
|--|--|--|--|--|--|--|--|--|--|

SRINIX COLLEGE OF ENGINEERING

3rd INTERNAL EXAMINATION 2021-22

Sub – Math-III

sem-3rd

Branch - All

Full marks- 100

Time – 2.30hrs

1. Answer all questions (Part – A)

(2 x 10 =20)

- What is Independent event?
- Explain the gauss quadrature formula.
- Define probability distribution function.
- What is Newton's forward interpolation formula.
- Define one-tail and two-tail testing.
- What is Diagonally dominant matrix?
- If A and B are two events such that $P(A)=1/4, P(B)=1/2, P(AB)=1/8$ find $P(\text{not A and not B})$
- State the Baye's theorem.
- Distinguish between binomial and poisson distribution.
- What is expectation of a random variable?

2. Answer any eight questions (Part – B)

(6x8=48)

- Solve by Crout's method the system of equation
$$\begin{aligned}x+2y+3z &= 14 \\2x+ 5y+ 2z &= 18 \\3x+ 2y+ 3z &= 22\end{aligned}$$
- Solve Numerically $dy/dx = y-x$, where $y(0) = 2; h = 0.1$; Find $y(0.1)$ by Runge – kutta method of order 4.
- A black and red die are rolled.find the conditional probability of obtaining a sum greater than 9, the given that the black die resulted in a 5.
- A bag contains 4 red and 4 black balls,another bag contains 2 red and 6 black balls.one of the two bags is selected at random and a ball is drawn from the bag which is found to be red.find the probability that the ball is drawn from the first bag.
- Use Newton's Raphson method find a root of the equation $xe^x-2=0$ correct to three decimal places.
- Fit a straight line $y=a+bx$ to the following data by the method of least square;

| | | | | | |
|---|----|----|----|----|----|
| x | 1 | 2 | 3 | 4 | 5 |
| y | 14 | 27 | 40 | 55 | 68 |

g) Using the Newton's divided difference formula calculate the value of $f(10)$ from the following data;

| | | | | |
|------|-----|----|-----|------|
| x | 4 | 7 | 9 | 12 |
| F(x) | -43 | 83 | 327 | 1053 |

h) Using the Newton's forward interpolation formula calculate the value of $f(3)$ from the following data

| | | | | | | |
|------|---|---|----|-----|-----|-----|
| x | 0 | 2 | 4 | 6 | 8 | 10 |
| F(x) | 0 | 4 | 56 | 204 | 496 | 980 |

D) Evaluate $\int_0^6 \frac{dx}{1+x^2}$ by using Simpson's $\frac{3}{8}$ rule.

3. Answer all two questions (Part – C) (16 x 2 = 32)

a) Find the correlation coefficient and the equation of the lines of regression for the following values of x and y

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| x | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| y | 2 | 4 | 7 | 6 | 5 | 6 | 5 |

b) Solve the following system of equations by using Gauss-seidel method

$$4x + y + 2z = 4$$

$$3x + 5y + z = 7, x + y + 3z = 3$$

c)

(i) Two ladies were asked to rank 7 different types of lipsticks. The ranks given by them are given below

| | | | | | | | |
|----------|---|---|---|---|---|---|---|
| Lipstick | A | B | C | D | E | F | G |
| Anita | 2 | 1 | 4 | 3 | 5 | 7 | 6 |
| Sunita | 1 | 3 | 2 | 4 | 5 | 6 | 7 |

Calculate Spearman's rank correlation coefficient

(ii) State and prove Baye's theorem.